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Females, the elderly, and also males: Demographic aging and macroeconomy in Japan $\stackrel{\star}{\sim}$



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ABSTRACT

The speed and magnitude of ongoing demographic aging in Japan are unprecedented. A rapid decline in the labor force and a rising fiscal burden to finance social security expenditures could hamper growth over a prolonged period. We build a dynamic general equilibrium model populated by overlapping generations of males and females who differ in participation rate, employment type and labor productivity as well as life expectancy. We study how changes in the labor market over the coming decades will affect the transition path of the economy and fiscal situation of Japan. We find that a rise in the labor supply of females and the elderly of both genders in an extensive margin and in labor productivity can significantly mitigate effects of demographic aging on the macroeconomy and reduce fiscal pressures, despite their negative effects on equilibrium wages during the transition. The study suggests that a combination of policies that remove obstacles hindering labor supply and that enhance a more efficient allocation of male and female workers of all age groups will be critical to keeping government deficit under control and raising income across the nation.

1. Introduction

Japan is experiencing rapid and massive demographic aging. Despite the imminent urgency to deal with macroeconomic and fiscal concerns, how Japan is going to handle a dramatic shift in its demographic structure and rising expenditures remains to be seen.

In this paper, we build a general equilibrium model of overlapping generations of male and female individuals and quantify effects of demographic trends affecting the future path of individual behaviors, macroeconomic variables and fiscal situations in Japan.

The Japanese government is keen on encouraging labor force participation of females and nowadays also of the elderly. The employment rate for prime-age males is above 90% and there is not much room to further increase their participation. Females and the elderly are two groups of individuals whose participation is lower than that of primeage males and who could contribute more, thereby slowing down the expected decline in aggregate labor supply and potentially improving the fiscal situation. What is unknown, however, is whether and how a rise in labor supply of females and the elderly by a given magnitude affects the Japanese economy including the transition path of output and factor prices as well as fiscal tensions associated with rising social security expenditures. Our focus is to quantify effects of changes in the labor supply, treated exogenously in the paper, of individuals of different genders, age as well as employment types and productivity.

We find that a rise in participation of females and the elderly, for example, as projected by the Japan Institute for Labour Policy and Training (JILPT), could significantly mitigate a massive decline in the labor force and its consequences on macroeconomy expected during the coming decades. Quantitative effects, however, are most significant when not only labor force participation rates but also distribution of employment types as well as their productivity measured in terms of their wages also grow, for example, to the levels of males.

Many female workers in their late 20s and 30s leave the labor force when they marry and have children. A large number of them return to work after several years, yielding a so-called "M-shaped" profile of participation rates over the life-cycle. When they return, however, their

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employment types often differ from the ones prior to their departure and most of them are engaged in a contingent job rather than a regular job. The former typically pays significantly less than the latter. There also exists also a major gap between male and female wages even after controlling for age and employment type. Our study suggests that efforts to narrow the gap between males and females in the dimensions of participation rate, employment type and wage, would go far in making up for the decline in the labor force and filling the gap between rising government expenditures and shrinking revenues.

Although much focus in the policy discussion is on females and the elderly and this paper is not an exception, there are some concerning trends in the labor supply of males during recent years. Among primeage working males, there has been a rise in the fraction of contingent workers across age groups from their 20s to 50s. The trend can be observed since the early 2000s at least, when a breakdown of employment types among workers became available from the Labor Force Survey (LFS). Similarly to females, contingent workers have much lower earnings compared to regular workers of the same gender. We find that aggregate labor supply, as well as capital and output, will be much lower and the fiscal burden in terms of tax rates needed to finance rising expenditures will be higher, if the trend of a rising share of contingent workers among males continues.

Our study is an extension of general equilibrium models of overlapping generations to study life-cycle allocations of individuals, in the tradition of Auerbach and Kotlikoff (1987). We follow literature that uses such models to study effects of cross-generational redistributional policies, such as De Nardi et al. (1999), Conesa and Krueger (1999), Nishiyama and Smetters (2007), and Kitao (2014). There are studies that use a life-cycle model to analyze effects of aging demographics and fiscal challenge in Japan, including Hansen and Imrohoroğlu (2016), Braun and Joines (2015), Kitao (2015), Hoshi and Ito (2014), Doi et al. (2011), Okamoto (2013).

These papers abstract from differences between males and females and assume life-cycle profiles of wages and demographics of either males or an average of the two groups. The two, however, have very different profiles of labor market experience over their life-cycle as mentioned above. Work by imrohoroğlu et al. (2016, 2019) presents a generational accounting model with details of employment types of males and females, as well as institutional structures of the Japanese social security system. The studies, however, assume partial equilibrium and differ from ours in that we explicitly incorporate production and endogenous determination of factor prices driven by the ongoing demographic aging.

This paper, however, does not present a model to investigate why gender gaps in terms of labor market experience of males and females exist, or why females are sorted to particular employment types initially and also later in their life-cycle. While these are important issues, this paper's focus is to quantify the effects of exogenous changes in the pattern of labor supply, extrapolating the trend in several possible ways, on the future path of the macroeconomy, factor prices and fiscal situations. We aim to identify factors that are critical in projections of these variables in a general equilibrium framework of males and females.

Papers such as Attanasio et al. (2008), Blundell et al. (2016) build a model with endogenous female labor supply and study their life-cycle behavior, taking into account gender heterogeneity within families. Recent work by Blundell et al. (2019) extends these models and estimates a structural life-cycle model to evaluate roles of formal training and experience for females in mitigating the wage gap between men and women. They show that effects of training can be important especially for women who have fewer years of education. Lise and Yamada (2018) estimate a structural model of intra-family allocations of consumption and time used for leisure, home production and market work, using a unique panel dataset of Japanese households. Extending the current paper in such a direction in the context of the Japanese economy and over a long time-horizon will be a challenging but

promising direction of future work.

The rest of the paper is organized as follows. We present the model in Section 2. Details of the calibration and data sets used are given in Section 3. The benchmark results and various sensitivity analyses are discussed in Section 4. Section 5 concludes.

2. The model

In this section, we describe the model, the problem of individuals and the definition of a competitive equilibrium. Details of the computation of the transition dynamics are provided in Appendix A.

2.1. Demographics

We let *t* denote time, *i* age of an individual with a maximum age of *I*. *g* denotes the gender, taking one of two values $\{m, f\}$, representing male and female, respectively. The model is populated by overlapping generations of individuals of gender *g* who enter the economy at age i = 1. $s_{i,g,t}$ denotes the probability that an individual of gender *g* alive at time t - 1 at age i - 1 survives until the next period. Unconditional probability of surviving *i* periods up to time *t* is given by

$$S_{i,g,t} = \prod_{k=1}^{i} s_{k,g,t+(k-i)}$$

 $S_{1,g,t} = s_{1,g,t} = 1$ and $S_{l+1,g,t} = s_{l+1,g,t} = 0$ for all g and t. We denote by $\mu_{i,g,t}$ the size of the population of age i, gender g and at time t. The size of a new cohort $\mu_{1,g,t}$ grows at rate $n_{g,t}$.

2.2. Technology

Output is produced according to a constant returns to scale (CRS) aggregate production function, $Y_t = F(Z_t, K_t, N_t)$. Output can be used for consumption or investment. Z_t denotes the total factor productivity at time t, N_t is the aggregate labor supply and K_t is the aggregate capital. Capital depreciates at a constant rate δ each period. Firms are competitive and interest rate and wage equal marginal products of capital and labor, respectively. We assume that the level of productivity grows exogenously at rate λ_t .

2.3. Preferences and endowments

Individuals' instantaneous utility function is given as

$$u(c_{i,g,t}) = \frac{c_{i,g,t}^{1-\Theta}}{1-\Theta},\tag{1}$$

where $c_{i,g,t}$ denotes consumption of an individual of age *i* and gender *g* at time *t*. Individuals of gender *g* born at time *t* choose the optimal path of consumption and saving in order to maximize their lifetime utility given as

$$U_{g,t} = \sum_{i=1}^{I} \beta^{i-1} S_{i,g,t+i-1} \frac{c_{i,g,t+i-1}^{1-\theta}}{1-\theta}.$$
(2)

 β denotes a subjective discount factor. Assets that are accidentally left by the deceased are distributed as a lump-sum transfer to all surviving individuals and the amount is denoted as b_t .

Individuals of age *i* and gender *g* at time *t* exogenously supply $\varepsilon_{i,g,t}$ efficiency units of labor in the market. They receive the market wage w_t for each unit of efficiency. Before-tax earnings are given as $\varepsilon_{i,g,t} w_t$.

We let $a_{i,g,t}$ denote assets held by an individual of age *i* and gender *g* at time *t*. We assume that individuals enter the economy with no initial assets, that is, $a_{1,g,t} = 0$. We allow individuals to borrow and impose no borrowing constraint during their lifetime, except that they cannot have negative assets at the end of their last age *I*, that is, $a_{l+1,g,t} = 0$.

2.4. Government

The government raises revenues through taxes on consumption at rate $\tau_{c,b}$ labor income at $\tau_{w, b}$ and capital income at $\tau_{a,b}$ and issuance of risk-free debt, B_{t+1} . Government borrowing and tax revenues finance a stream of expenditures, G_b benefits of the PAYG social-security program and payment of debt, $(1 + r_i)B_i$.

We assume that individuals are entitled to public pension benefits once they reach the normal retirement age (NRA), I^R . Note that this is the age to become eligible to receive pensions and not necessarily the age to leave the labor force. We let $p_{i,g,t}$ denote public pension benefits that individuals of age *i* and gender *g* receive at time *t*. We assume that social security benefits are determined by the formula

$$p_{i,g,t} = \kappa_t \frac{W_{i,g,t}}{I^R - 1},$$

where κ_t is the replacement ratio of average past earnings. Cumulated past gross earnings $W_{i,g,t}$ are defined recursively as

$$W_{i,g,t} = \begin{cases} \varepsilon_{1,g,t} w_t & \text{if } i = 1\\ \varepsilon_{i,g,t} w_t + W_{i-1,g,t-1} & \text{if } 1 < i < I^R\\ W_{i-1,g,t-1} & \text{if } i \ge I^R. \end{cases}$$
(3)

The government budget constraint reads as

$$G_{t} + (1 + r_{t})B_{t} + \sum_{i=I^{R}}^{I} \sum_{g} p_{i,g,t}\mu_{i,g,t} = \tau_{w,t}w_{t} \sum_{i=1}^{I} \sum_{g} \mu_{i,g,t}\varepsilon_{i,g,t} + \tau_{a,t}r_{t} \sum_{i=1}^{I} \sum_{g} \mu_{i,g,t}(a_{i,g,t} + b_{t}) + \tau_{c,t} \sum_{i=1}^{I} \sum_{g} \mu_{i,g,t}c_{i,g,t} + B_{t+1}.$$
(4)

In the simulations, we let either the labor income tax rate $\tau_{w, t}$ or consumption tax rate $\tau_{c,t}$ in (4) adjust to achieve a budget balance in each period *t*. More details about calibration of the tax rates and assumptions we make for fiscal policy during the transition are given in Section 3.

2.5. Individuals' Problem

The problem faced by an individual is to choose a sequence of consumption and saving at each age so that the objective function defined in Eq. (2) is maximized. We formulate a recursive problem below. An individual's state vector at each time period is given as $\{i, g, a\}$, where *i* is age, *g* gender and *a* assets. The value function $V_t(i, g, a)$ of an individual in state $\{i, g, a\}$ at time *t* is given as follows.

$$V_t(i, g, a_t) = \max_{c_t, a_{t+1}} \{ u(c_t) + \beta s_{i+1, g, t+1} V_{t+1}(i+1, g, a_{t+1}) \}$$

subject to

$$(1 + \tau_{c,t})c_t + a_{t+1} = (1 - \tau_{w,t})\varepsilon_{i,g,t}w_t + [1 + (1 - \tau_{a,t})r_t](a_t + b_t) + p_{i,g,t}.$$
(5)

where $p_{i,g,t}$ denotes pensions and is zero for individuals aged below I^{R} .

2.6. Competitive equilibrium

A competitive equilibrium, for a given sequence of demographics, total factor productivity levels $\{Z_t\}_{t=1}^{\infty}$, and fiscal variables $\{G_t, B_t, \tau_{a,t}, \tau_{w,t}, \kappa_t, \{p_{i,g,t}\}_{i,g}\}_{t=1}^{\infty}$, is a sequence of¹

- individuals' choices $\{\{c_{i,g,t}, a_{i,g,t}\}_{t=1}^{\infty}\}_{t=1}^{\infty}$
- consumption tax rates $\{\tau_{c,t}\}_{t=1}^{\infty}$,
- wage rates $\{w_t\}_{t=1}^{\infty}$, interest rates $\{r_t\}_{t=1}^{\infty}$, and
- aggregate variables $\{K_t, N_t\}_{t=1}^{\infty}$

such that:

- Individuals choose sequences of consumption and saving, maximizing the objective function in (2) subject to the budget constraint (5).
- 2. Firms maximize profits by equating the marginal product of each input with its price, i.e.

$$w_t = F_N(Z_t, K_t, N_t), \tag{6}$$

$$r_t = F_K(Z_t, K_t, N_t) - \delta.$$
⁽⁷⁾

3. The lump-sum transfer of accidental bequests equals the amount of assets left by the deceased, distributed equally to all surviving individuals.

$$b_t = \frac{\sum_{i=1}^{I-1} \sum_g a_{i+1,g,t} (1 - s_{i+1,g,t}) \mu_{i,g,t-1}}{\sum_{i=1}^{I} \sum_g \mu_{i,g,t}}$$

4. The labor market clears at wage w_t and aggregate labor supply is given by

$$N_t = \sum_{i=1}^{I} \sum_{g} \mu_{i,g,t} \varepsilon_{i,g,t}.$$
(8)

5. The bond and capital markets clear at interest rate r_{t} , and the aggregate stock of capital satisfies

$$K_t + B_t = \sum_{i=1}^{l} \sum_{g} \mu_{i,g,t} (a_{i,g,t} + b_t).$$
(9)

- 6. The tax rate $\tau_{c,t}$ satisfies the government budget constraint (4).
- 7. The goods market clears.

$$\sum_{i=1}^{l} \sum_{g} \mu_{i,g,t} c_{i,g,t} + K_{t+1} + G_t = F(Z_t, K_t, N_t) + (1 - \delta)K_t$$
(10)

3. Calibration

In this section, we describe parametrization of the model and various data sources that we use to calibrate the model. The transition starts in an economy, which approximates the Japanese economy in 1990. We call this economy the initial steady state. A final steady state is computed, where the demographic transition is complete and all variables, including demographics and micro and macro variables, have become stationary.² We then let the economy make a transition between the two steady-states, by imposing the projected path of demographics. The model frequency is annual.

3.1. Demographics

We let individuals enter the economy at age i = 1, which

¹ The equilibrium definition is based on the scenario in which consumption tax rates are adjusted along the transition. When the period government budget constraint is satisfied with another policy tool, such as labor income taxes, equilibrium definition needs to be modified accordingly.

 $^{^{2}}$ In the computation, we set the final year of the transition to 2500, which needs to be far enough so that all variables converge to those in the final steady state smoothly.

corresponds to 20 years old, and live up to the maximum model age of I = 85, or 104 years old. We use demographic projections of the National Institute of Population and Social Security Research (IPSS) for age and gender-specific survival rates, $s_{i,g,t}$, and growth rates of a new cohort, $n_{g,t}$ ³ In computation of the baseline transition, we use population projections based on medium scenarios of fertility rates and survival rates. In Section 4.2.2, we consider low and high scenarios of both demographic parameters and study sensitivity of our results to alternative population projections.

3.2. Preferences

A parameter of relative risk aversion θ is set at 2.0. The subjective discount factor β is set at 1.046 so that the model achieves a capitaloutput ratio of 3.2 in 2015, which is based on the average ratio of the sum of tangible and intangible fixed assets and GDP between 2010 and 2014.4

3.3. Technology

We assume a constant returns to scale production function,

$$F(Z_t, K_t, N_t) = Z_t(K_t)^{\alpha} (N_t)^{1-\alpha}.$$

The capital share parameter α is set at 0.40 and the depreciation rate of capital δ at 7% per year, based on the values reported in the Actuarial Valuation of the Ministry of Health, Labour and Welfare (MHLW) in 2014.⁵In the baseline simulation, λ_t , the annual growth rate of the total factor productivity (TFP), which is Z_{tr} is set to 1.0% throughout the transition periods.⁶We consider alternative scenarios for the growth rate of TFP in Section 4.2.

3.4. Employment and wages

In our model, $\varepsilon_{i,g,t}$ denotes efficiency units supplied to the labor market by a group of individuals of age *i*, gender *g* at time *t*. As such, it is considered as a composite of average efficiency units of workers of age i and gender g that also depends on their labor force participation rate. The former, the average efficiency units, are an average of workers in heterogeneous types of employment.

Fig. 1 shows labor force participation rates of males and females by age, based on the Labor Force Survey (LFS) in 2015. In the figure, labor force participation rate is defined as the number of employed workers in the labor market divided by the number of all individuals of each gender and age.7

Among males, participation rates are high and stay above 90% in their mid-20s to mid-50s. Participation rates start to decline thereafter.



Note that, however, they do not reach zero until long after they turn 65, the normal retirement age (NRA) of the public pension, or even 70.

Participation rates are lower among females than males at almost all ages, and the profile shows two humps in their mid-20s and more mildly in their late 40s and early 50s, exhibiting a so-called "M-shaped" profile of participation. A large number of female workers leave the labor force when they become married and start raising children and then return to work after a certain number of years.⁸

Typically, however, they do not return to the same position when they resume working and earnings are often lower than those before they left the labor force. Many females return to work as contingent workers, rather than regular workers. On a regular job, employment is more stable, typically continuing without an explicit end or even lasting for a lifetime until the retirement age set by a firm. Contingent jobs include part-time jobs or employment with a fixed-term contract and such earnings in general are much lower than those in regular jobs. In addition to regular and contingent jobs, there are also self-employed workers.

Fig. 2 shows the population distribution of working individuals of males and females over the life-cycle, by the workers' employment type.⁹

Fig. 3 shows earnings profiles of male and female workers of different employment types. For regular and contingent workers, average earnings are computed based on the Basic Survey of Wage Structure (BSWS) data.¹⁰ For self-employed individuals, there are no earnings data in the BSWS and we use data from the Employment Status Survey (ESS).¹¹

Using above statistics, efficiency units $\varepsilon_{i,g,t}$ of individuals of age *i* and gender g are computed as weighted average of earnings:

$$\varepsilon_{i,g,t} = (y_{i,g,t}^R \mu_{i,g,t}^R + y_{i,g,t}^C \mu_{i,g,t}^C + y_{i,g,t}^S \mu_{i,g,t}^S) / \mu_{i,g,t},$$
(11)

where $y_{i,g,t}^R$, $y_{i,g,t}^C$ and $y_{i,g,t}^S$ denote before-tax earnings of regular, contingent and self-employed individuals of age *i* and gender *g*,

³ The official demographic projection under various scenarios can be obtained at the website of the IPSS. http://www.ipss.go.jp/pp-zenkoku/e/zenkoku_ e2017/pp_zenkoku2017e.asp

⁴The data is from the SNA. https://www.esri.cao.go.jp/jp/sna/data/data_ list/kakuhou/files/h26/h26_kaku_top.html (in Japanese).

⁵ The average depreciation rate is 7.1% in 2003-2012 (or 7.5% in 1983-2012) and capital ratio 42.8% in 2003-2012 (or 40.8% in 1983-2012), based on https://www.mhlw.go.jp/stf/seisakunitsuite/bunya/0000093204. html (in Japanese, Chapter 3-4).

⁶ The average TFP growth rate was 0.9% in 2010–2015, according to the estimates of the Monthly Economic Report of the Cabinet Office. The growth was much higher in 1980s at 2.1%, falling to 1.2% in 1990s and 0.9% in 2000s.

⁷ Note that we do not include unemployed individuals and family workers (kazoku jugyosha) in computing labor force participation rates. Family workers are members of a self-employed individual's household, who help the business but do not receive wage. Unemployment rates have been low, with the average of 3.7% between 2010 and 2018, standing at 2.4% in 2018. Consistently, when we simulate alternative scenarios of participation using the projections in Section 4, we use those of age and gender specific employment rates, not including family workers and unemployed individuals.

⁸ As we discuss in Section 4, the M-shape has become less visible in recent years. The Japan Institute for Labour Policy and Training (JILPT) projects that the profile will become even flatter over the next 20 years.

[&]quot;Regular" workers include regular (seiki) workers and managers (yakuin) and "contingent" contains irregular (hiseiki) workers including part-time workers, contracted workers and temporary staff. The LFS data is released by the Statistics Bureau of the Ministry of Internal Affairs and Communications (MIC).

¹⁰ The BSWS data is available at: https://www.mhlw.go.jp/english/database/ db-l/wage-structure.html

¹¹ The ESS is a survey conducted every five years. We use earnings data of 2017 and adjust the level using the CPI. https://www.e-stat.go.jp/stat-search/ file-download?statInfId = 000031729381&fileKind = 0



Fig. 2. Labor force participation rates by employment type (% of total population at each age).



Fig. 3. Earnings by employment type (in million JPY).



respectively. To compute profiles used in the baseline simulations, we use data at time t = 2015. $\mu_{i,g,t}^R$, $\mu_{i,g,t}^C$ and $\mu_{i,g,t}^S$ are the number of individuals of each type. Fig. 4 shows profiles of average efficiency, $\varepsilon_{i,g,t}$, for males and females. In the baseline simulation, we assume that the age-efficiency profile for each gender is time-invariant. In Section 4.2, we consider alternative scenarios about participation rates, employment type distribution and earnings in the future, and evaluate their effects on macroeconomic and fiscal projections.

3.5. Government

Public pension system

The government operates a pay-as-you-go pension system. The normal retirement age I^R is set at 46 in the baseline simulation, which corresponds to 65 years old. The replacement rate κ_t is determined in equilibrium so that total pension expenditures in 2015 correspond to 9.5% of GDP in that year and the calibrated value is 0.534. Both I^R and κ_t are fixed throughout the transition of the baseline simulation.¹²

Debt, government expenditures and taxes

 $^{^{12}\,\}rm We$ simulate alternative paths of these policy parameters and results are available in online appendix.

The government debt B_t is set to 156% of GDP, which corresponds to the net debt of the consolidated government at the central and local levels. It is computed by subtracting the value of financial assets held by the central and local governments from the value of their total gross debt in 2015. G_t is determined so that the ratio of government expenditures to GDP is 20% as in the data of the central and local governments in 2015.

For the revenue side, we set the tax rate on capital income $\tau_{a,t}$ at 35% in line with the estimates of effective tax rates in the literature.¹³ We let the consumption tax rate $\tau_{c,t}$ follow the actual path in the past up to 2020, increasing from 8% to 10% in late 2019 and in 2020.¹⁴ While consumption taxes increase deterministically until 2020, $\tau_{w,t}$ is determined in equilibrium to balance the budget in each year. In the baseline simulation, the labor income tax rate in equilibrium is in the range of 36–39% in the 2010s, which is in line with estimates in the literature.¹⁵ Note that this tax encompasses all taxes imposed on labor income, including social security taxes.

After 2020, we assume that consumption taxes are adjusted in each period to balance the government budget and keep the labor income tax rate constant at its equilibrium value in 2020, which is 37.7%. In Section 4.2.4, we consider an alternative financing scheme, in which labor income taxes are adjusted throughout the transition, holding consumption tax rate fixed at 10% after 2020.

4. Numerical analysis

In this section, we present numerical results of our baseline simulations and other experiments. Our focus is to analyze effects of changes in the labor supply, especially by females and the elderly (although we show males are also important), on the path of the macroeconomy, as well as the impact of alternative scenarios about demographic transition, productivity and fiscal policies. Before we present and discuss these scenarios, we will first examine and characterize the baseline transition, in which we assume that there is no change in labor supply profiles of individuals or government policy, except for the tax rates to balance the government budget in each period, and that demographics follow official projections of the IPSS according to its medium scenarios of fertility rates and survival probabilities.

4.1. Baseline simulations

Fig. 5 shows the paths of aggregate capital and labor supply in the baseline transition between 2015 and 2070.¹⁶ Labor supply declines immediately and sharply as the size of the working-age population falls by more than 20% by 2040, 30% by 2050 and 40% by the mid-2060s. We also note and emphasize that female contribution to aggregate labor, as measured by total efficiency units, is significantly smaller than that of males. In 2015, more than 70% of total labor is supplied by males and less than 30% by females. It implies that if females in an equal number as males were to supply the same efficiency units as males, total labor supply could rise by about 40%, though of course, how wage would adjust in response to the more abundant labor supply

¹³ Hansen and İmrohoroğlu (2016) use the method of Hayashi and Prescott (2002) and estimate the capital income tax rate in 2010 at 35.6%

 14 The consumption tax rate was raised to 10% in October 2019. Since our model frequency is annual, we assume that the tax rate increases from 8% in 2018 to 8.5% in 2019 and then to 10% in 2020 in the computation.

¹⁵ Gunji and Miyazaki (2011) estimate average marginal tax rates on labor income.

remains to be seen. In Section 4.2, we consider various experiments to explore channels through which the gap between male and female experience in the labor market is narrowed and we analyze how other variables will respond to changes in the labor market.

Aggregate capital does not decline as sharply as labor supply initially since a rise in longevity will give incentives to accumulate more wealth for a longer period of retirement, which offsets the decline driven by a fall in the number of savers. The latter effect, however, starts to dominate quickly with the wave of retirement of the second baby boomers, the generation born in the early 1970s. Aggregate capital falls by approximately 15% by the mid-2040s and 30% by 2060.

As a result of the unsynchronized decline in aggregate capital and labor, the capital labor ratio initially rises until the late 2040s and falls thereafter. Fig. 6 shows the paths of factor prices, the wage rate and interest rate, between 2015 and 2070. The wage rate will rise initially as labor supply becomes scarcer relative to capital and begin to fall gradually in the late 2040s. The interest rate will decline by about one percentage point between 2015 and the late 2040s and rise slightly thereafter.

As shown in Fig. 7, the equilibrium consumption tax rate starts to adjust endogenously after 2020 and increases rapidly to finance rising expenditures in response to demographic aging. It rises by about 14 percentage points from 2020 to 2070 in the baseline transition. The sizeable increase in consumption taxes required to finance the demographic transition is in the range of estimates in the literature.¹⁷

4.2. Labor force participation and alternative scenarios

In this section, we simulate the economy under alternative scenarios about various economic assumptions we imposed along the baseline transition path.

4.2.1. Labor force participation (males, females, and the elderly)

We consider scenarios about labor force participation of individuals of different characteristics. The government is keen on encouraging more participation, especially that of females as well as the elderly. These are two groups of individuals whose participation is much lower than that of prime-age males and who are considered to have the potential to contribute to a rise in the aggregate labor supply and potentially improve fiscal situations.

Fig. 8 shows projections of labor force participation rates by the Japan Institute for Labour Policy and Training (JILPT) in 2025 and 2040, together with the data of the Labor Force Survey (LFS) in 2002 and 2015.¹⁸ The projections are often used as underlying parameters in official economic and fiscal forecasts in Japan.¹⁹ The overall

¹⁶ For the rest of the paper, reported variables are stationarized by the longrun growth rate. More precisely, aggregate capital, output, consumption and wage rates are stationarized by the growth rate of $\lambda/(1 - \alpha)$. There is no adjustment for aggregate labor supply since we assume that the population growth rate will converge from current negative values to zero in the long-run.

¹⁷ The figures, however, are higher in some recent papers such as Kitao (2015) and Braun and Joines (2015), partly because we do not explicitly take into account medical and long-term care expenditures, which are part of the focus of these papers.

¹⁸ The LFS started in the late 1940s and provides labor force data for long periods. As discussed below, 2002 is the first year that the survey includes information about employment types so we can compare the transition of participation rates and distribution by employment types consistently.

¹⁹ The projections are available on the JILPT website: https://www.jil.go.jp/ english/index.html (English) and https://www.jil.go.jp/kokunai/statistics/ rouju.html (Japanese). Labor force participation rates for 2015 are based on the data from the Labor Force Survey (LFS). In computing participation rates for 2015, we take the ratio of the sum of regular, contingent and self-employed workers to the population. We exclude unpaid "family workers" (*kazoku jugyosha*) from the definition of participation since by definition they do not receive wages in the same way as other individuals who supply labor domestically without being paid. We assume the same for these projections (which implicitly include those family workers) and subtract the same fraction of "family workers" as in 2015 from the estimates to derive consistent figures of labor force participation rates. The numbers are relatively small and such treatment does not affect projections in a significant way.



Fig. 5. Baseline transition: aggregate variables. Levels are normalized by the aggregate value in 2015.



Fig. 6. Baseline transition: factor prices. Wages are normalized by the value in 2015.



participation rate has been rising, mainly driven by an increase in the participation of females and the elderly during the past decades. The projections assume that this trend will continue for the next few decades.

As shown in Fig. 9, which plots the difference between projections and data in 2015 to highlight growth, the projections assume a rapid rise in participation of both male and female elderly above age 65 as well as a major increase in labor supply of females across essentially all ages, but, in particular, during their child-bearing ages of 30s to 40s. We will use these projections of the JILPT in the analysis of alternative scenarios about labor force participation in the future. Details of various scenarios about labor force participation are summarized in Table 1.

Female labor force participation (LFP)

As described in Section 3, there are significant differences between males and females in their labor market experience. First, they differ in participation rates over the life-cycle. Second, distribution of employment types is different. Third, earnings are much higher for males, even controlling for age and employment type.

We simulate scenarios in which these differences are mitigated and the gap eventually disappears during the transition. According to the projections by the JILPT, female participation rates will rise monotonically over the next few decades and reach levels that are still below



Fig. 8. Labor force participation rate projections (2025 and 2040, JILPT) and data (2002 and 2015, LFS) .



Fig. 9. Labor force participation rate projections: change from 2015.

Table 1 Description of labor force participation (LFP) scenarios.

-	
Scenario	Assumptions
LFP-1	Female LFP rise from 2015 to 2040, based on JILPT projections.
LFP-2	LFP-1 plus convergence of employment type to males'.
LFP-3	LFP-2 plus convergence of efficiency to males'.
LFP-4	Same as LFP-1 but only aged 65 and below.
LFP-5	Female and male LFP rise from 2015 to 2040, based on the JILPT projections.
LFP-6	A rise of contingent workers among males aged 65 and below. Trend in 2002–2015 extended to 2041.
LFP-7	A rise of contingent workers among males of all ages. Trend in 2002–2015 extended to 2041

but closer to those of males, as shown in Fig. 8.

In the first experiment, **LFP-1**, we assume that female participation rates by age will rise as projected by the JILPT. We assume that efficiency units provided by females of different ages will be the same on average, that is, the composition of employment type and efficiency units of participating females remains unchanged.

In the second experiment, **LFP-2**, we assume the same path of rising participation rates as in the first experiment, but we let the distribution of employment types gradually converge toward that of males by 2040.

In the third experiment, **LFP-3**, we assume that labor efficiency units by age and employment type will also converge toward those of males by 2040.

Both tax revenues and expenditures of the government will change under alternative scenarios about labor force participation in the future. We adjust consumption tax rates after 2020 to balance the government budget. By comparing paths of consumption taxes required to achieve the budget balance, we are able to evaluate how alternative scenarios about primitives or policies will affect the fiscal burden associated with aging demographics. We make the same adjustment by consumption taxation in other experiments presented in this section.²⁰

Fig. 10 shows the paths of aggregate labor supply, capital and output under the three scenarios as well as those of the baseline transition. They clearly show that more participation of females will effectively increase labor inputs. What would, however, generate a more

²⁰ Note that throughout the transition we keep all other taxes including labor income taxes fixed at the same level as in the baseline simulations and the only change in the fiscal parameter will be that of the consumption tax rate in each period. In experiments, the budget balance is imposed only after 2020 by endogenous consumption taxes. Alternatively, one could also adjust consumption taxes prior to 2020 counterfactually but our main quantitative results about the future transition paths will not be affected in any significant way.

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Fig. 10. Female labor supply: aggregate variables .

significant impact is not simply a rise in labor force participation, but also changes in how they participate and contribute to production. As shown in Fig. 10a, the labor supply will rise by significantly more if there is also convergence in employment type and efficiency.

Fig. 10c shows that the economy would produce more with a larger number of females participating in the labor force, and the effects are larger under the LFP-2 and 3 scenarios. Given a projected rise in income due to more participation, individuals reduce savings initially to smooth the path of consumption, which is reflected in the initial decline in aggregate capital in Fig. 10b relative to the baseline scenario. Aggregate capital, however, will eventually be higher than in the baseline transition as the economy becomes more productive and individuals start to save more with additional resources.

Fig. 11 shows the paths of factor prices and consumption tax rates in the three scenarios of female labor supply and the baseline scenario. With a rise in female participation, labor will become more abundant relative to capital, and wages will be lower than in the baseline and even decline after 2015. The effect is intensified by an initial decline in capital. Gradually, however, capital will rise and labor will become scarcer. By 2070, wages under the three scenarios align to the level in the baseline model.

Fig. 11c shows more participation by females will significantly reduce the fiscal burden. By 2045, equilibrium tax rates will be lower by 1.5, 3.3 and 5.8 percentage points than in the baseline simulations. Although more participation will lower wage rates during the transition and could potentially reduce the tax base, higher labor supply dominates in the net effect. In addition, aggregate output will be higher during the transition and tax revenues from other sources will rise and help reduce fiscal costs of demographic aging.

As shown in Fig. 8, female labor force participation is projected to rise among both the young and the elderly. In order to isolate effects of rising participation rates of the elderly, we consider a scenario, LFP-4, in which we let female participation rates increase as projected by the JILPT, just as in scenario LFP-1, but a rise is restricted to those aged 65 and below. Changes between the baseline and LFP-4 highlight the effects of rising participation among younger females. The difference between LFP-1 and 4 indicates effects of rising participation of elderly females.

For males, although there is not much room for a further increase in the participation rate in their prime age, a major increase is projected among elderly males as highlighted in Fig. 9. We simulate a scenario, LFP-5, in which we assume that participation rates of both males and females follow the path as projected by the JILPT. The difference between LFP-1 and 5 highlights effects of rising participation of (mostly elderly) males.

Fig. 12 shows the paths of aggregate labor, wage and equilibrium consumption tax rate under the two scenarios of LFP-4 and 5 and the baseline. Paths of LFP-1 are also included in the figures to facilitate comparison.

Difference in aggregate labor between LFP-1 and 4 in Fig. 12a is the contribution resulting from the rise in participation among elderly females aged 65 and above. Although their participation rates are much higher by 2040, effects on labor supply are not very large (see Table 2 for percentage changes in selected years across scenarios). This is because a large fraction of elderly females in the labor force are contingent workers, whose labor supply in terms of efficiency units is significantly lower than that of regular workers. Much larger effects are expected if the distribution of employment types as well as their efficiency units also change as we saw in scenarios LFP-2 and 3. As a result,



Labor force participation of the elderly and males

Fig. 11. Female labor supply: wage, interest rate and consumption tax rate.

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(a) Labor

(b) Wage

2040

2050

2030

(c) Tax rate (%)

2040

2050

Baseline

2070

I FP-1

I FP-

I FP-5

2060

Fig. 12. Labor supply: males and the elderly.

nd the elderly.

24 22

20

18

16 14

12

10

g

2020

2030

Baseline

2070

I FP-1

.... LFP-4

=1 FP-5

2060

Table 2Labor force participation (LFP) scenarios.

Year	LFP-1	LFP-2	LFP-3	LFP-4	LFP-5	LFP-6	LFP-7		
Labor (% change relative to baseline in each year)									
2030	5.61	12.10	22.36	4.70	8.46	-2.00	-2.58		
2045	7.75	18.80	37.73	5.99	11.92	-3.44	-4.77		
2060	7.48	18.65	37.67	6.01	11.37	-3.47	-4.59		
Capital	Capital (% change from baseline in each year)								
2030	-0.67	-1.49	-3.76	0.01	-2.16	0.44	1.14		
2045	3.75	9.20	16.47	3.89	3.59	-1.52	-1.15		
2060	6.18	16.49	31.32	6.04	6.47	-2.87	-2.74		
Output	Output (% change from baseline in each year)								
2030	3.05	6.45	11.15	2.80	4.08	-1.03	-1.11		
2045	6.13	14.87	28.80	5.15	8.51	-2.68	-3.34		
2060	6.96	17.78	35.09	6.03	9.38	-3.23	-3.85		
Wage (% change from baseline in each year)									
2030	-2.42	-5.04	-9.16	-1.82	-4.04	0.99	1.51		
2045	-1.50	-3.31	-6.49	-0.80	-3.05	0.79	1.50		
2060	-0.49	-0.73	-1.87	0.01	-1.79	0.25	0.77		
Interest	Interest rate (ppt change from baseline in each year)								
2030	0.45	0.97	1.86	0.33	0.76	-0.18	-0.27		
2045	0.26	0.60	1.22	0.14	0.55	-0.14	-0.26		
2060	0.09	0.13	0.34	-0.00	0.32	-0.04	-0.13		
Consumption tax rate (ppt change from baseline in each year)									
2030	-1.12	-2.46	-4.19	-0.98	-1.48	0.50	0.62		
2045	-1.47	-3.34	-5.77	-1.14	-2.07	0.70	0.99		
2060	-1.29	-2.79	-4.79	-0.86	-2.00	0.73	1.11		

changes in wages and tax rates are also smaller as shown in Fig. 12b and 12c.

A rise in the male participation rate will increase aggregate supply more significantly, which can be seen by comparing the path of labor supply under **LFP-1** and **5** in Fig. 12a. Effects on wage and tax rate are also larger as shown in Fig. 12b.

Employment types of males - regular vs contingent

Although labor force participation rates of prime-age males are high and there is little room for participation rates to rise further, there is a somewhat concerning trend in employment type among participating males.

Fig. 13 shows shares of regular, contingent and self-employed male workers out of all male workers at each age in 2002, the first year when breakdown by employment type is available in the Labor Force Survey (LFS), and in 2015. Among prime-age individuals, there is some shift of workers from regular jobs to contingent jobs. More precisely, a fraction of contingent workers increased at almost all ages throughout the lifecycle between 2002 and 2015, while a fraction of regular workers declined at ages between the mid-20s and mid-40s. The trend implies lower average efficiency supplied by male workers of these age groups and lower earnings. A rise in the number of male workers engaged in contingent jobs, which typically provide a stream of less stable and lower income, has been debated as a concerning trend, which may also imply insufficient accumulation of wealth during the working period and for retirement and, at the same time, insufficient entitlement to public pension benefits (see, for example, Kitao and Yamada, 2019).

We simulate a scenario, **LFP-6**, in which this trend of rising contingent male workers continues until 2041. More precisely, we let an average rise in the fraction of contingent workers aged 65 and below, observed during the 13 years between 2002 and 2015, continue for another 26 (=13 × 2) years until 2041 and assume that regular workers are replaced by the same fraction. In **LFP-7**, we also consider a case where the same shift occurs across all age groups, including those aged above 65.²¹

Fig. 14 shows the paths of labor supply, wage and equilibrium consumption tax rate under LFP-6 and 7. Aggregate supply will be lower if the trend continues, by more than 3% in LFP-6 relative to the baseline by 2045 and by almost 5% under LFP-7. Wage will be higher with scarcer labor supply, though the effects are relatively small since saving and aggregate capital decline at the same time. Given a lower output and tax base, equilibrium tax rates will be slightly higher.

Summary of labor force participation scenarios

Details of the seven scenarios of labor force participation are summarized in Table 1. Table 2 shows changes in selected aggregate variables relative to levels in the baseline model for each of the experiments.

An increase in participation of not only females but also males will raise labor inputs, but larger effects are identified when employment types of females and their efficiency contributions also change and trend closer to those of males. More participation will lower wage rates compared to the baseline simulation initially, but a rise in savings and aggregate capital will eventually reverse the direction.

More participation, despite a transitional fall in wage rates, will increase economic activities and expand the tax base, which leads to a lower equilibrium tax rate under all five scenarios of rising participation, **LFP-1** to **5**. **LFP-6** and **7** show the opposite effect on tax rate and imply that the ongoing trend of changes in employment type and earnings of male workers is something that we also need pay careful attention to.

²¹ We also simulated other scenarios including one replacing self-employed workers with contingent workers. The effects are not large quantitatively since the difference in earnings of contingent and self-employed individuals is not as great as between these two groups and regular workers. Results are available from authors upon request.

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(b) Contingent

(c) Self-employed

Fig. 13. Employment types of male workers in 2002 and 2015 (% of all employed). Labor force survey (LFS).



Fig. 14. Labor supply: employment types of males.

4.2.2. Demographic projections

In the baseline simulations, we used demographic projections of the IPSS under the medium scenario. They also report projections based on high and low scenarios for fertility rates and survival rates, respectively. To assess sensitivity of our results to demographic assumptions, we compute the transition based on the four alternative scenarios of low and high cases of fertility and survival rates.

Fig. 15 shows simulation results under three scenarios for fertility rates: low, medium (baseline) and high. Even if fertility rates start to rise or fall immediately, a change in labor supply is not visible until around 2040, when a larger (or smaller) number of newborns start to

participate in the labor market. Higher fertility implies more abundant labor and lower wages, though the difference is relatively small even in 2070. A larger labor force with higher fertility also implies less fiscal burden while additional newborns are in the labor force and the equilibrium tax rate is lower by about 1 percentage point in 2050 and 3 percentage points in 2070.

Fig. 16 shows simulation results under low, medium (baseline) and high scenarios for survival rates. With a high survival rate, individuals expect to live longer and are incentivized to save more for a longer retirement period, even before they reach retirement age. Fig. 16c shows that equilibrium tax rates are similar across three scenarios until





30 25 20 15 10 Low fertility ····· High fertility 5 2020 2030 2040 2050 2060 2070 (c) Tax rate (%)

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around the mid-2030s but they are higher in the medium and long-run when survival rates are higher and individuals live longer. Tax revenues initially increase with a rise in wage rates but pension expenditures are higher in the long-run and so are equilibrium tax rates to finance additional expenditures.

4.2.3. Total factor productivity growth

In the baseline economy we assume that total factor productivity (TFP), Z_{t_0} grows at a constant rate of 1%. In this section, we consider alternative scenarios of lower and higher TFP growth.

Fig. 17 shows the paths of capital, equilibrium tax rate, interest rate and wage when the TFP grows at 0.5%, 1.0% (baseline) and 1.5%. For capital and wage rate, levels are adjusted by the same rate as the growth rate to stationarize the baseline transition so that levels of these variables are comparable in the same figure.

All else being equal, a steeper income profile implies a lower saving rate at the individual level. For aggregate capital, however, such effects are partially offset by a rise in the level of disposable income. As shown in Fig. 17a, aggregate capital is lower initially but eventually grows faster if the economy is able to sustain high growth. Fiscal burden, which is expressed in terms of the equilibrium tax rate, will be lower in a high-growth economy since tax revenues continue to grow at a higher rate and equilibrium tax rates are lower.

Interest rate is determined by both the level of TFP and capital-labor ratio and stays higher in the experiment in a high growth economy, as shown in Fig. 17c. Wages grow faster with higher growth, as shown in Fig. 17d.

4.2.4. Alternative fiscal scenarios

Bequest taxation

In the baseline model, we assume that accidental bequests are confiscated and transferred in entirety to all surviving individuals. In this section, we study effects of incorporating in the model inheritance tax on bequeathed assets. We assume that all bequests are subject to proportional bequest taxation at rate τ_b and calibrate the tax rate so the model matches the size of total bequest tax revenues as in the data, which stood at 0.424% of GDP in 2018 based on the data of the Ministry of Finance. The calibrated bequest tax rate is 9.4%.²²

As shown in Fig. 18c, bequest tax will raise additional revenues and equilibrium consumption tax rates will be lower than in the baseline scenario, although the change is small and within a range of less than one percentage point. Aggregate capital is slightly lower than in the baseline and interest rates are higher as shown in Fig. 18b.

Labor income taxes

In the baseline model, we use consumption taxes to balance the

government budget during the transition. In this section, we simulate the model assuming that labor income taxes are adjusted to finance the demographic transition while the consumption tax remains unchanged at 10% after 2020. As shown in Fig. 19c, equilibrium labor income tax rates rise from about 38% to above 52% by 2070, increasing by a similar magnitude in percentage points as a rise in consumption taxes in the baseline transition.

Aggregate capital, as shown in Fig. 19a declines similarly to the baseline transition, but it will fall by more as the tax burden has shifted more to labor income of younger individuals, who now have lower disposable income and save less. Wages under this simulation are lower with a decline in capital. Output will also decline faster compared to the baseline transition. We note that effects on aggregate economic activity may well be magnified in a model that endogenizes labor supply response to distortionary taxation and those demonstrated under this experiment may be considered as a lower bound of consequences of raising labor taxes to finance the demographic transition.

4.2.5. Labor supply elasticity

In our baseline model, labor supply is assumed to be exogenous throughout the transition. In this section, we consider a scenario in which labor supply of males and females will each respond to dynamics of wage rates, by the magnitude corresponding to labor supply elasticity estimated in the applied micro literature.

Kuroda and Yamamoto (2008) use multiple sources of data including the Survey on Time Use and Leisure Activities and the Basic Survey on Wage Structure (BSWS) and estimate labor supply elasticity in intensive and extensive margins for various socio-economic groups of individuals. We set the labor supply elasticity parameter of 0.45 and 1.40 for males and females, respectively, which are in the range of estimates of Kuroda and Yamamoto (2008) for intensive and extensive margins of labor supply using different data sets. In the computation, we let labor supply respond to a change in wage rates relative to that of 2015. A rise in wage rates implies an increase in labor supply relative to the baseline scenario.

Fig. 20a shows the path of labor supply relative to the baseline case. An increase in the labor supply in response initially reduces equilibrium wage as shown in Fig. 20b. The change, however, of wage rates is relatively small and eventually align with the level of the baseline simulations as individuals also increase saving and capital stock starts to rise. As shown in Fig. 20c, the fiscal burden is reduced by an increase in labor supply and equilibrium consumption tax rates lie slightly below those of the baseline model.

Our baseline model is also silent about effects of intra-family decisions of labor supply and consumption-saving allocations and does not distinguish between roles of males and females within a family. One may be concerned about effects of higher earnings of females on labor supply of their spouses, which may mitigate positive effects on aggregate economic activity that we identified from various experiments.

²²Source: https://www.mof.go.jp/tax_policy/summary/property/e02.htm (in Japanese)



Fig. 17. TFP growth rate scenarios.

Lise and Yamada (2018) build a structural model of intra-household allocations of consumption and time used for leisure, home production and market work, which is estimated using data from the Japanese Panel Survey of Consumers (JSPS). They estimate effects of an increase in wages of an individual on consumption and time allocations of himself/herself as well as those of the spouse. Their results indicate a very small, if any, effect of a rise in female wages on her husband's time for market work. Therefore we would consider that negative effects on males' labor supply caused by a trend of rising female wages are likely to be limited, although such elasticities may as well change when allocations of time within family, especially that related to home production, evolve over time.

5. Conclusion

With the unprecedented magnitude and speed of demographic aging, Japan faces an urgent need to present a policy path that makes its fiscal situation and macroeconomy sound and stable. In this paper, we build a general equilibrium model of individuals of different age and gender, who optimally choose a life-cycle path of consumption and

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5.6 24 Baseline Baseline Baseline 0.95 22 Bequest ta Bequest tax Bequest tax 5 4 20 0.9 5.2 0.85 18 0.8 5 16 0.75 14 4.8 0.7 12 4.6 10 0.65 0.6 44 ۶ 2070 2020 2030 2040 2050 2060 2020 2030 2040 2050 2060 2070 2020 2030 2040 2050 2060 2070 (c) Tax rate (%)(a) Capital (b) Interest rate (%) Fig. 18. Bequest tax. 1.06 55 Baseline Endoge nous labor ta 0.9 1.04 50 0.8 1.02 45 0.7 40 0.98 0.6 aseline Endogenous labor tax Endogenous labor tax 0.5 0.96 35 2020 2030 2040 2050 2060 2070 2020 2030 2040 2050 2060 2070 2020 2030 2040 2050 2060 2070 (a) Capital (b) Wage (c) Labor income tax (%)Fig. 19. Endogenous labor income tax. 1.06 24 22 0.9 1.05 0.8 20 1.04 18 0.7 Male: baseline 1.03 Male: elastic labo 16 0.6 Female: baseline 1.02 male: elastic lab 14 0.5 1.0 12 0.4 0.3 10 Baseline Baseline Elastic labor supply Flastic labor supply 0.2 0.99 2020 2030 2040 2050 2060 2070 2020 2030 2040 2050 2060 2070 2020 2030 2040 2050 2060 2070 (c) Tax rate (%)(a) Labor supply (b) Wage

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en- the projection.

Fig. 20. Elastic labor supply.

We find that a rise in female labor force participation has large positive effects on aggregate labor supply, output and eventually wages and reduces the fiscal burden and tax rate necessary to finance rising expenditures. Effects are, however, much more significant if not only participation rates but also employment type and productivity of each female worker relative to that of a male worker rise. Many women work on a contingent job rather than a regular job, and the latter provides a significantly higher stream of income than the former. Similarly, a rise in the number of the elderly in the labor force, both males and females, will be effective, but quantitative effects also depend on how they participate in the labor market. Our study suggests that policies to stimulate labor force participation of females and the elderly will be effective and the government also needs to consider ways to remove

saving given a sequence of income, policy and other economic environmental factors. We considered alternative scenarios of the transition, focusing particularly on different assumptions about inclusion of females and the elderly in the labor force, as well as other assumptions about demographic projections, productivity growth and fiscal policies.

Females and the elderly are two groups of individuals in Japan whose labor supply could further rise and help mitigate effects of a massive decline in the labor force during the coming decades due to demographic aging. The contribution of female workers constitutes less than 30% of the total labor supply as of 2015, measured in terms of total wage income. We use official projections of the Japan Institute for Labour Policy and Training (JILPT) on labor supply of males and females across different ages and quantify effects on the macroeconomy and fiscal situation in Japan if participation rates change according to

over a life-cycle will be important. Such a model will enable various normative and positive analysis of policies that affect work incentives of

females, including distortionary taxation and those related to social security or human capital formation. Second, given the rapid rise in the

number of the elderly expected during the coming decades, it is important to analyze how their ability and incentives to work interact

with policies in the context of aging economy. Third, participation

decisions of females are connected to intra-family decisions such as

marriage, child bearing and an allocation of time to home and market

production. A model that disentangles such interactions will be essen-

tial in considering not only positive effects of female participation on

aggregate labor supply and output that we identified in the paper but

also tradeoffs involved in terms of within-family activities and ex-

ternalities to other family members. We leave these interesting and

important issues for future research.

obstacles for them from choosing jobs that provide more stable and higher earnings.

Although challenges tend to receive more emphasis than bright hopes in analyses of the Japanese macroeconomy and fiscal situation in the future, this paper identifies untapped or under-used potential resources in the labor market and demonstrates their large effects. Our analysis implies that a combination of policies to remove obstacles hindering labor supply and to enhance a more efficient allocation of male and female workers across age groups will be critical to keeping government deficit under control and raising income across the nation and that such policies should be implemented without further delay.

We conclude by noting some directions of research that the current paper implies are highly promising. First, building a model that fully endogenizes labor supply decisions of both males and females and that explains the peculiar pattern and the trend of participation of females

Appendix A. Computation of the transition dynamics

We compute the transition path following the four steps described below.

Step 1: Compute the initial and final steady-states of the model. The computation of the steady state economy is essentially the same as that described in Step 3 below, without time subscripts since all variables are stationary.

Let the economy make the transition from the initial steady state to the final steady state over *T* periods. Set *T* large enough so that all variables converge smoothly to the values in the final steady state.

Step 2: Guess three vectors of the three equilibrium variables, which are aggregate capital, wage tax rate, and accidental bequests, in each period of the transition.

Given the path for aggregate capital, using the properties of constant returns to scale technology and optimization conditions for firms, sequences of interest rates and wages can be derived.

Step 3: Given the paths of factor prices, tax rates and accidental bequests obtained in Step 2, solve individuals' optimization problem. Recall that the budget constraint of an individual at time *t* is given as follows

$$(1 + \tau_{c,t})c_{i,g,t} + a_{i+1,g,t+1} = y_{i,g,t} + R_t(a_{i,g,t} + b_t)$$

where $y_{i,g,t}$ denotes total after-tax income of an individual of age *i* and gender *g* at time *t*, which includes after-tax labor income and public pension benefits for those aged at and above I^R . R_t denotes net-of-tax gross interest rate, $R_t \equiv 1 + (1 - \tau_{a,t})r_i$. The Euler equation for asset holdings next period implies the optimal growth rate of consumption between age *i* and *i* + 1 as

$$\frac{c_{i+1,g,t+1}}{c_{i,g,t}} = \left[\beta s_{i+1,g,t+1} \frac{1+\tau_{c,t}}{1+\tau_{c,t+1}} R_{t+1}\right]^{\frac{1}{6}} \equiv \gamma_{i+1,g,t+1}^c.$$
(12)

 $\gamma_{i,g,t}^c$ is the growth rate of consumption of an individual of age *i* and gender *g* from time *t* to *t* + 1 (and age *i* + 1). Iterating backward over (12), we obtain:

$$c_{i+1,g,t+i} = c_{1,g,t} \prod_{k=1}^{i} \gamma_{k+1,g,t+k}^c$$

The discounted present value of the total (gross of taxes) lifetime consumption expenditures of an individual of age 1 at time t is given as

$$\bar{c}_{1,g,t} = c_{1,g,t} \left[(1 + \tau_{c,t}) + \sum_{i=1}^{l-1} (1 + \tau_{c,t+i}) \prod_{k=1}^{i} \frac{s_{k+1,g,t+k}}{R_{t+k}} \gamma_{k+1,g,t+k}^{c} \right].$$
(13)

The discounted present value of the total (gross of taxes) lifetime consumption expenditures of an individual of age i^* at time t is

$$\overline{c}_{i^*,g,t} = c_{i^*,g,t} \left[\left(1 + \tau_{c,t} \right) + \sum_{i=i^*}^{I-1} \left(1 + \tau_{c,t+(i-i^*+1)} \right) \prod_{k=i^*}^{i} \frac{s_{k+1,g,t+(k-i^*+1)}}{R_{t+(k-i^*+1)}} \gamma_{k+1,g,t+(k-i^*+1)}^c \right].$$
(14)

The discounted present value of the total (net of taxes) lifetime income of an individual of age 1 and gender g at time t is:

$$\bar{y}_{1,g,t} = y_{1,g,t} + \sum_{i=1}^{I-1} \left(\prod_{k=1}^{i} \frac{s_{k+1,g,t+k}}{R_{t+k}} \right) y_{i+1,g,t+i}.$$
(15)

The discounted present value of the total (net of taxes) lifetime earnings of an individual of age i^* and gender g at time t is:

$$\overline{y}_{i^*,g,t} = y_{i^*,g,t} + \sum_{i=i^*}^{I-1} \left(\prod_{k=i^*}^{i} \frac{s_{k+1,g,t+k}}{R_{t+(k-i^*+1)}} \right) y_{i+1,g,t+(i-i^*+1)} + R_t a_{i^*,g,t}.$$
(16)

Since individual optimization requires $\bar{c}_{i^*,g,t} = \bar{y}_{i^*,g,t}$ for each age i^* and time t, from (14) and (16), we obtain $c_{i^*,g,t}$ as

$$c_{i^*,g,t} = \frac{\overline{\mathcal{Y}}_{i^*,g,t}}{\left[(1 + \tau_{c,t}) + \sum_{i=i^*}^{I-1} (1 + \tau_{c,t+(i-i^*+1)}) \prod_{k=i^*}^{i} \frac{s_{k+1,g,t+(k-i^*+1)}}{R_{t+(k-i^*+1)}} \gamma_{k+1,g,t+(k-i^*+1)}^c \right]}$$

Note that $a_{i^*,g,t}$ in Eq. (16) is computed residually from $c_{i^*-1,g,t-1}$ and the budget constraint (5):

$$a_{i^*,g,t} = y_{i^*-1,g,t-1} + R_{t-1} \left(a_{i^*-1,g,t-1} + b_{t-1} \right) - (1 + \tau_{c,t-1}) c_{i^*-1,g,t-1}.$$

Step 4: Aggregating asset holdings of all age groups and genders, we obtain the implied sequence of aggregate capital and accidental bequests. We update a guess for the sequence of aggregate capital and bequests. We use government budget constraints (4) to update our guess for the tax rate. If convergence is not reached, we restart from Step 3 with a new vector of guesses.

Supplementary material

Supplementary material associated with this article can be found, in the online version, at 10.1016/j.jjie.2020.101064

References

- Attanasio, O.P., Low, H., Sánchez-Marcos, V., 2008. Explaining changes in female labour supply in a life-cycle model. Am. Econ. Rev. 98 (4), 1517–1552.
- Auerbach, A.J., Kotlikoff, L.J., 1987. Dynamic fiscal policy. Cambridge University Press, Cambridge.
- Blundell, R., Costa-Dias, M., Goll, D., Meghir, C., 2019. Wages, experience and training of women over the lifecycle. Cowles Foundation Discussion Paper No. 2174.
- Blundell, R., Dias, M.C., Meghir, C., Shaw, J., 2016. Female labor supply, human capital, and welfare reform. Econometrica 84 (5), 1705–1753.
- Braun, R.A., Joines, D., 2015. The implications of a greying Japan for public policy. J. Econ. Dyn. Control 57, 1–23.
- Conesa, J.C., Krueger, D., 1999. Social security with heterogeneous agents. Rev. Econ. Dyn. 2 (4), 757–795.
- De Nardi, M., İmrohoroğlu, S., Sargent, T.J., 1999. Projected U.S. demographics and social security. Rev. Econ. Dyn. 2 (3), 575–615.
- Doi, T., Hoshi, T., Okimoto, T., 2011. Japanese government debt and sustainability of fiscal policy. J. Jpn. Int. Econ. 25 (4), 414–433.
- Gunji, H., Miyazaki, K., 2011. Estimates of average marginal tax rates on factor incomes in Japan. J. Jpn. Int. Econ. 25 (2), 81–106.
- Hansen, G.D., İmrohoroğlu, S., 2016. Fiscal reform and government debt in Japan: aneoclassical perspective. Rev. Econ. Dyn. 21, 201–224.

- Hayashi, F., Prescott, E.C., 2002. The 1990s in Japan: a lost decade. Rev. Econ. Dyn. 5 (1), 206–235.
 Hoshi, T., Ito, T., 2014. Defying gravity: can the Japanese sovereign debt continue to
- increase without a crisis? Econ. Policy 29 (77), 5–44.
- İmrohoroğlu, S., Kitao, S., Yamada, T., 2016. Achieving fiscal balance in Japan. Int. Econ. Rev. 57 (1), 117–154.
- İmrohoroğlu, S., Kitao, S., Yamada, T., 2019. Fiscal sustainability in Japan: What to tackle? J. Econ. Ageing 14 Article 100205. Forthcoming
- Kitao, S., 2014. Sustainable social security: four options. Rev. Econ. Dyn. 17 (4), 756–779. Kitao, S., 2015. Fiscal cost of demographic transition in Japan. J. Econ. Dyn. Control 54, 37–58
- Kitao, S., Yamada, T., 2019. Dimensions of inequality in Japan: Distributions of earnings, income and wealth between 1984 and 2014. Working Paper.
- Kuroda, S., Yamamoto, I., 2008. Estimating Frisch labor supply elasticity in Japan. J. Jpn. Int. Econ. 22 (4), 566–585.
- Lise, J., Yamada, K., 2018. Household sharing and commitment: evidence from panel data on individual expenditures and time use. Rev. Econ. Stud. 17 (4), 582–612.
- Nishiyama, S., Smetters, K., 2007. Does social security privatization produce efficiency gains? Q. J. Econ. 122 (4), 1677–1719.
- Okamoto, A., 2013. Welfare analysis of pension reforms in an ageing Japan. Jpn. Econ. Rev. 64 (4), 452–483.